

Statistics

Lecture 6



Feb 19-8:47 AM

Class QZ 7

Box Your Final Ans.

Given Regression line $y = 45 - 8x$, $\sum y = 50$, $n = 5$

Predict y when $x = 4$ is

1) r is significant.

use regression line $y = 45 - 8(4) = 45 - 32 = \boxed{13}$

2) r is not significant.

use $\bar{y} = \frac{\sum y}{n} = \frac{50}{5} = \boxed{10}$

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Class QZ 6
 use the chart below

x	y
5	12
6	15
6	18
7	20
4	10
8	20

Find

$a = -.967 \approx \boxed{-1}$ } $y = 3x - 1$
 $y = -1 + 3x$
 Round to whole #

$b = 2.8 \approx \boxed{3}$

$r^2 = .883 \approx \boxed{88\%}$ } Round to whole %

$r = \boxed{.939}$ } Round to 3-decimal

x → DL1
 y → DL2

STAT → **CALC**
8: LinReg(a+bx)

Xlist: L1
 Ylist: L2

Clear
Calculate

Mar 5-9:05 PM

Intro. to probabilities (SG 10)

$E \rightarrow$ Desired event (outcome)

$P(E) \rightarrow$ Prob. that E happens

Acceptable Answers:

- 1) Reduced fraction
- 2) Round to 3-decimal places
- 3) Scientific Notation

$$P(E) = \frac{\text{Total \# of all desired outcomes}}{\text{Total \# of all outcomes}}$$

ex: A box has 10 Red and 15 Blue balls.
 If we randomly select one ball, find the Prob. that it is red.

$P(\text{Red}) = \frac{10}{25}$ total red balls / total balls

$P(\text{Red}) = \frac{2}{5}$

10 ÷ 25 **Math** **1: Frc** **Enter**
Math **2: Dec** **Enter**

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A standard deck of playing cards has 52 cards, 26 red, 12 face cards, and 4 aces.

If we randomly draw one card, find the Prob. of getting

1) Red

$$P(\text{Red}) = \frac{26}{52} = \boxed{\frac{1}{2}} = \boxed{.5}$$

2) Face card

$$P(\text{Face}) = \frac{12}{52} = \boxed{\frac{3}{13}} \approx \boxed{.231}$$

3) ace

$$P(\text{Ace}) = \frac{4}{52} = \boxed{\frac{1}{13}} \approx \boxed{.077}$$

4) Red ace

$$P(\text{Red ace}) = \frac{2}{52} = \boxed{\frac{1}{26}} = \boxed{.038}$$

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$E \rightarrow$ Desired Event

$P(E) \rightarrow$ Prob. that E happens

$\bar{E} \rightarrow$ Not E , E -bar, E Complement

$$P(E) + P(\bar{E}) = 1 \quad \text{Complement Rule}$$

$$P(\bar{E}) = 1 - P(E)$$

A box has 10 Red, 15 Blue, and 5 white color balls. Suppose we randomly select one ball,

$$1) P(\text{Red}) = \frac{10}{30} = \boxed{\frac{1}{3}} \approx \boxed{.333} \quad 2) P(\bar{\text{Red}}) = 1 - P(\text{Red}) = 1 - \frac{1}{3} = \boxed{\frac{2}{3}} \approx \boxed{.667}$$

$$3) P(\text{Red or Blue}) = \frac{25}{30} = \boxed{\frac{5}{6}} \quad 4) P(\text{Red and Blue}) = \frac{0}{30} = \boxed{0}$$

Do not use \emptyset for 0.

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John has a birthday next week. Find the prob. that his birthday happens on Tuesday.

$$\frac{1 \text{ Tuesday}}{7 \text{ Days}} = \boxed{\frac{1}{7}}$$

Find the prob. that today is Majid's birthday.

$$\frac{1 \text{ day}}{365 \text{ Days}} = \frac{1}{365}$$

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Some Prob. Rules & Terms:

1) $0 \leq P(E) \leq 1$

2) Sum of all prob. of all possible events is always 1.

3) $P(E) = 1 \iff$ Sure event

4) $P(E) = 0 \iff$ Impossible event

5) $0 < P(E) \leq .05 \iff$ Rare event

6) $P(\bar{E}) = 1 - P(E)$ Complement Rule

$$P(\text{Rains}) = .25 \quad P(\overline{\text{Rain}}) = 1 - P(\text{Rains}) \\ = 1 - .25 = \boxed{.75}$$

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Did You Vote Last week? I surveyed 80 people

	Yes	No	Total
Male	20	15	35
Female	10	35	45
Total	30	50	80

If we randomly select one of them,

1) $P(\text{Male}) = \frac{35}{80} = \frac{7}{16}$

2) $P(\text{Yes}) = \frac{30}{80} = \frac{3}{8}$

3) $P(\text{Male and Yes}) = \frac{20}{80} = \frac{1}{4}$

4) $P(\text{Male or Yes}) = \frac{45}{80} = \frac{9}{16}$

SG 10

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Addition Rule:

Keyword: OR

Single Action event

ex: $P(A) = .3$, $P(B) = .8$, $P(A \text{ and } B) = .25$

$P(\bar{A}) = 1 - P(A) = 1 - .3 = .7$

$P(\bar{B}) = 1 - P(B) = 1 - .8 = .2$

$P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B) = 1 - .25 = .75$

$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$

$= .3 + .8 - .25 = .85$

$P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .85 = .15$

SG 11

↑
Overlap
A & B
together

Complement
Rule

↑
Addition
Rule

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$$P(HB) = .45$$

$$1) P(\overline{HB}) = 1 - .45 = \boxed{.55}$$

$$P(FF) = .35$$

$$2) P(\overline{FF}) = 1 - .35 = \boxed{.65}$$

$$P(HB \text{ and } FF) = .25$$

$$3) P(HB \text{ or } FF) = P(HB) + P(FF) - P(HB \text{ and } FF)$$

↑
Addition
Rule

$$= .45 + .35 - .25 = \boxed{.55}$$

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Mutually Exclusive Events
"Disjoint Events"

A & B are M.E.E. $\Leftrightarrow P(A \text{ and } B) = 0$

E: $P(A) = .32$, $P(B) = .6$, A & B are M.E.E.

$$1) P(\overline{A}) = 1 - P(A) = \boxed{.68}$$

$$2) P(\overline{B}) = 1 - P(B) = \boxed{.4}$$

$$3) P(A \text{ and } B) = \boxed{0}$$

$$3) P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) = .32 + .6 - 0 = \boxed{.92}$$

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Addition Rule with Venn Diagram

Total Prob. = 1

$P(A) = .4$, $P(B) = .7$, $P(A \text{ and } B) = .2$

$P(A \text{ only}) = .4 - .2 = .2$

$P(B \text{ only}) = .7 - .2 = .5$

Total = 1

$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$
 $= .4 + .7 - .2 = \boxed{.9}$

$P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .9 = \boxed{.1}$

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$P(A) = .1$

$P(B) = .5$

A & B are disjoint events

Total = 1

$P(\bar{A}) = \boxed{.9}$

$P(\bar{B}) = \boxed{.5}$

$P(A \text{ and } B) = \boxed{0}$

$P(A \text{ or } B) = .1 + .5 - 0 = \boxed{.6}$

$P(\overline{A \text{ or } B}) = \boxed{.4}$

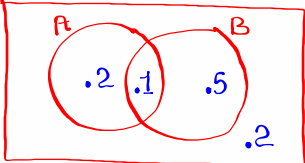
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De Morgan's Law:

$$P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B})$$

$$P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B})$$

$P(A) = .3$, $P(B) = .6$ $P(A \text{ and } B) = .1$
 $P(A \text{ only}) = .3 - .1 = .2$
 $P(B \text{ only}) = .6 - .1 = .5$



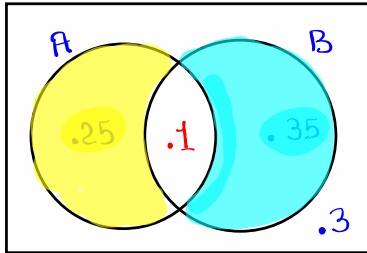
$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$ Total = 1
 $= .3 + .6 - .1 = \boxed{.8}$

$P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .8 = \boxed{.2}$
 De Morgan's Law

$P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B) = 1 - .1 = \boxed{.9}$

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Complete the Venn Diagram below



1) $P(A) = .35$
 2) $P(B) = .45$
 3) $P(A \text{ and } B) = .1$

Total Prob. = 1

4) $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) = \boxed{.7}$

5) $P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B}) = 1 - .7 = \boxed{.3}$
 De Morgan's Law

6) $P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B}) = 1 - .1 = \boxed{.9}$

7) $P(\text{A only OR B only}) = .25 + .35 = \boxed{.6}$
 ↑
 add

Mar 12-8:55 PM

Class QZ 8

class MP	class F
15	8
25	12
35	15
45	10
55	5

class MP \rightarrow L1class F \rightarrow L2

Find

$$1) \bar{x} = 33.4 \approx \boxed{33} \quad \left. \begin{array}{l} \text{Round to} \\ \text{whole \#} \end{array} \right\}$$

$$2) s = 12.182 \approx \boxed{12}$$

$$3) n = \boxed{50}$$

$$4) s^2 = \frac{\boxed{7272}}{\boxed{49}} \quad \left. \begin{array}{l} \text{Reduced} \\ \text{fraction} \end{array} \right\}$$

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